

Name:

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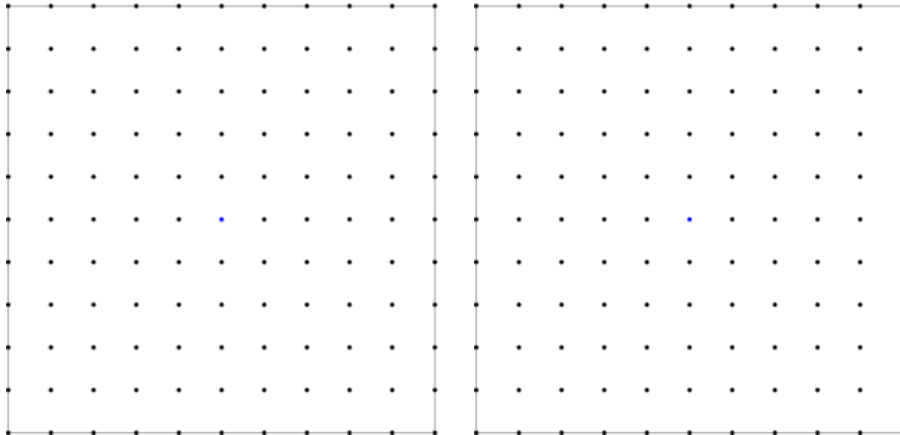
Pick's Theorem: Is it a fair representation of Lattice Polygons?

William Biersack

MTH 4040: Coordinating Seminar

Definition: A *lattice polygon* is a polygon where the vertices are elements of \mathbb{Z}^d for some $d \geq 2$

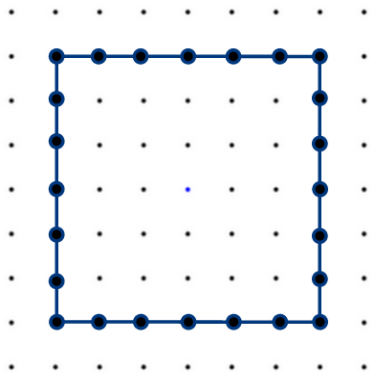
Practice creating lattice polygons!



Definition: Pick's Theorem

Given that A is the area of a closed lattice polygon, b is the number of lattice points on the polygon edges, and i is the number of points in the interior, then

$$A = i + \frac{1}{2} b - 1$$



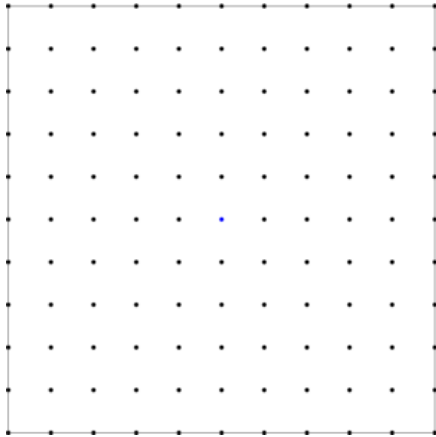
$$b = \underline{\hspace{2cm}} \quad i = \underline{\hspace{2cm}}$$

$$A = \underline{\hspace{2cm}} + \frac{1}{2} (\underline{\hspace{2cm}}) - 1$$

$$A =$$

Is this answer correct? How can we check it?

Let's try again! This time with a different polygon!



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$$A = \underline{\hspace{2cm}} + \frac{1}{2} (\underline{\hspace{2cm}}) - 1$$

$$A =$$

Check...